

Some *SCHUR*TM Examples: Using the **RULE** command

The **RULE** command in *SCHUR*TM can be a powerful tool in implementing algebraic formulae. Here we proceed through an advanced example, namely constructing a function that will evaluate the branching rule for

$$O(35) \rightarrow O(5) \times O(7) \quad (1)$$

The function may then be run for any mixed spinor irrep $[\Delta; \lambda]$ irrep of $O(35)$. Changing just three lines in the function gives results for and branching rule of the type

$$O(4rs + 2r + 2s + 1) \rightarrow O(2r + 1) \times O(2s + 1) \quad (2)$$

The basic branching rule follows from use of the results given in the paper

R. C. King, *J. Phys. A:Math. Gen.* **8**, 429 (1975)

$$[\Delta; \lambda] \rightarrow \sum_{\varepsilon, \zeta, \nu, \rho} [\Delta; ((s^r/\varepsilon\nu) \cdot ((\lambda/E \circ \zeta)/F\nu))] \times [\Delta; ((\tilde{\varepsilon}/\rho) \cdot (\zeta/F\rho))] \quad (3)$$

The above formula appears somewhat formidable and yet may be readily implemented in *SCHUR*TM using the function given below for the decomposition indicated in Eq. (1):-

```

rep
gr o35
enter rv1
dim rv1
setrich_spin rv1
exit
gr4o5o5o7o7
rule[3^2*rv1*0*0]sk2with e
rule last sum sk1conj3
rule last sum i2eq4
rule last sum sk1sk2
rule last sk2with f
contract1,2outer last
ch_spin gr1last
std_o gr1last
rule last sum sk2sk3
rule last sk3with f
contract2,3outer last
ch_spin gr2last
supoutpt false
std_o gr2last
dim last
stop

```

The numbers to the left of the function entries are solely for explanation here and DO NOT belong to the function. Let us now look closely at the above function. The first 6 rows are devoted to computing the dimension of the $O(35)$ irrep. Row 1 switches *SCHUR*TM to the REPMODE. Row 2 specifies the group as $O(35)$. Row 3 asks the user to enter an irrep of $O(35)$ e.g. $[\Delta; 31]$ would be entered simply as s31. Row 4 computes the dimension of the irrep. Row 5 removes the spin index from s31 and now $rv1 = 31$. Row 6 then returns *SCHUR*TM to the DPMODE.

Row 7 resets the group as $O(5) \times O(5) \times O(7) \times O(7)$. Thus we have $s = 3$ and $r = 2$. `rv1` plays the role of λ in Eq. (3). Row 8 now instructs **SCHUR**TM to do an S -function skew of the irrep of the second $O(5)$ group, treated as a S -function, with the S -function series E .

Row 9 instructs **SCHUR**TM to take the last result and skew $s^r = 3^2$ with the S -function series P . Row 10 then takes the last result and sums the effect of forming the skew of the "irrep" associated with the first group and the conjugate for the third group. That accomplishes the sum over the variable ε in Eq. (3). Row 11 does the corresponding sum over the variable ζ with $i2$ forming the inner product. We are now ready to carry out the sum over the variable ν as in Row 12 and then in Row 13 form the appropriate skew with the series D .

We have now completed the calculation for the two $O(5)$ groups and must combine the resulting S -functions under the operation of outer S -function multiplication to produce a list of single S -functions appropriate to tensor irreps of $O(5)$. The groups now appear as $O(5) \times O(7) \times O(7)$. We must now convert the $O(5)$ irreps into spinor irreps by first skewing the S -functions with the series Q via Row 15 and then inserting the spin index s via Row 16. This produces a list of $O(5) \times O(7) \times O(7)$ irreps with the $O(5)$ irreps not necessarily standard. These are made standard by issuing the command in Row 17.

The commands in Rows 18 to 23 complete the corresponding operations for $O(7)$. Row 24 instructs **SCHUR**TM to print to screen all further results. Had we placed Row 24 at the start of the function all actions would have been brought to the screen. Such an action can be helpful in testing a function. Row 25 completes the standardisation of the $O(7)$ irreps leaving the final result of the decomposition.

Row 26 computes the dimension of the resultant irreps which should agree with that found at the execution of Row 4. The final Row 27 stops the function. Below we give the voluminous output for the case considered here as an example. Running the function, here named `618.fn`, proceeds in **SCHUR**TM as follows:-

```
(If you wish to EXIT, enter END)
(If you wish to obtain HELP, enter ?help)
DPrep Mode (with function)
DP>
->readfn1'618.fn'
==
==
==
==
==
==
DP>
->fn1
REP mode
Group is 0(35)
enter rv1
->s31
dimension=23084400640
DPrep Mode (with function)
Group is 0(35)
Groups are 0(5) * 0(7) * 0(7)
Groups are 0(5) * 0(7)
```

where input instructions are indicated by $->$. The initial output is shown and the final output below has been produced as a table using **SCHURTM**'s \TeX commands. NB. Note that some of the coefficients of irreps are *negative* even though the dimension is computed correctly. As noted by King in his paper "The ambiguity in the distinction between spinor representations of $O(2k+1)$ and their associates is carried over into these expressions".

$O(35) \rightarrow O(5) \times O(7)$ decomposition for $[s31]$

$$\begin{array}{llll}
[s; 73][s; 31] & + [s; 73][s; 3] & + [s; 73][s; 21] & + 2[s; 73][s; 2] \\
+ [s; 73][s; 1^2] & + 2[s; 73][s; 1] & + [s; 73][s; 0] & + [s; 72][s; 41] \\
+ [s; 72][s; 4] & + [s; 72][s; 32] & + [s; 72][s; 31^2] & + 2[s; 72][s; 31] \\
+ 3[s; 72][s; 3] & + [s; 72][s; 2^2] & + [s; 72][s; 21^2] & + 4[s; 72][s; 21] \\
+ 4[s; 72][s; 2] & + [s; 72][s; 1^3] & + 3[s; 72][s; 1^2] & + 4[s; 72][s; 1] \\
+ 2[s; 72][s; 0] & + [s; 71][s; 42] & + [s; 71][s; 41^2] & + [s; 71][s; 41] \\
+ [s; 71][s; 4] & + [s; 71][s; 321] & + [s; 71][s; 32] & + 2[s; 71][s; 31^2] \\
+ 4[s; 71][s; 31] & + 2[s; 71][s; 3] & + [s; 71][s; 2^21] & + 2[s; 71][s; 2^2] \\
+ 4[s; 71][s; 21^2] & + 5[s; 71][s; 21] & + 4[s; 71][s; 2] & + 3[s; 71][s; 1^3] \\
+ 4[s; 71][s; 1^2] & + 3[s; 71][s; 1] & + [s; 71][s; 0] & + [s; 7][s; 421] \\
+ [s; 7][s; 41^2] & + [s; 7][s; 41] & + [s; 7][s; 321] & + [s; 7][s; 32] \\
- [s; 7][s; 31^2]\# & + 4[s; 7][s; 21^2] & + 2[s; 7][s; 31] & + [s; 7][s; 3] \\
+ 2[s; 7][s; 2^21] & + [s; 7][s; 2^2] & - [s; 7][s; 21^2]\# & + 5[s; 7][s; 21^2] \\
+ 4[s; 7][s; 21] & + [s; 7][s; 2] & - [s; 7][s; 1^3]\# & + 4[s; 7][s; 1^3] \\
+ 3[s; 7][s; 1^2] & + [s; 7][s; 1] & + [s; 64][s; 4] & + [s; 64][s; 31] \\
+ 2[s; 64][s; 3] & + [s; 64][s; 2^2] & + [s; 64][s; 21^2] & + 3[s; 64][s; 21] \\
+ 5[s; 64][s; 2] & + [s; 64][s; 1^3] & + 4[s; 64][s; 1^2] & + 6[s; 64][s; 1] \\
+ 4[s; 64][s; 0] & + [s; 63][s; 5] & + 3[s; 63][s; 41] & + 4[s; 63][s; 4] \\
+ 3[s; 63][s; 32] & + 3[s; 63][s; 31^2] & + 9[s; 63][s; 31] & + 12[s; 63][s; 3] \\
+ 2[s; 63][s; 2^21] & + 5[s; 63][s; 2^2] & + 6[s; 63][s; 21^2] & + 19[s; 63][s; 21] \\
+ 20[s; 63][s; 2] & + 7[s; 63][s; 1^3] & + 17[s; 63][s; 1^2] & + 22[s; 63][s; 1] \\
+ 11[s; 63][s; 0] & + 2[s; 62][s; 51] & + 2[s; 62][s; 5] & + 3[s; 62][s; 42] \\
+ 4[s; 62][s; 41^2] & + 8[s; 62][s; 41] & + 9[s; 62][s; 4] & + 2[s; 62][s; 3^2] \\
+ 5[s; 62][s; 321] & + 9[s; 62][s; 32] & + 11[s; 62][s; 31^2] & + 26[s; 62][s; 31] \\
+ 22[s; 62][s; 3] & + [s; 62][s; 2^3] & + 8[s; 62][s; 2^21] & + 16[s; 62][s; 2^2] \\
- [s; 62][s; 21^2]\# & + 24[s; 62][s; 21^2] & + 42[s; 62][s; 21] & + 37[s; 62][s; 2] \\
- [s; 62][s; 1^3]\# & + 20[s; 62][s; 1^3] & + 37[s; 62][s; 1^2] & + 37[s; 62][s; 1] \\
+ 17[s; 62][s; 0] & + [s; 61][s; 52] & + 2[s; 61][s; 51^2] & + 2[s; 61][s; 51] \\
+ 2[s; 61][s; 5] & + [s; 61][s; 43] & + 4[s; 61][s; 421] & + 4[s; 61][s; 42] \\
+ 8[s; 61][s; 41^2] & + 13[s; 61][s; 41] & + 8[s; 61][s; 4] & + 2[s; 61][s; 3^21] \\
+ 2[s; 61][s; 3^2] & + 2[s; 61][s; 32^2] & + 11[s; 61][s; 321] & + 16[s; 61][s; 32] \\
- 3[s; 61][s; 31^2]\# & + 28[s; 61][s; 31^2] & + 33[s; 61][s; 31] & + 23[s; 61][s; 3] \\
+ 3[s; 61][s; 2^3] & - 2[s; 61][s; 2^21]\# & + 21[s; 61][s; 2^21] & + 22[s; 61][s; 2^2] \\
- 6[s; 61][s; 21^2]\# & + 45[s; 61][s; 21^2] & - [s; 61][s; 21]\# & + 57[s; 61][s; 21] \\
+ 37[s; 61][s; 2] & - 7[s; 61][s; 1^3]\# & + 38[s; 61][s; 1^3] & - [s; 61][s; 1^2]\# \\
+ 45[s; 61][s; 1^2] & + 36[s; 61][s; 1] & + 14[s; 61][s; 0] & + [s; 6][s; 521] \\
+ 2[s; 6][s; 51^2] & + 2[s; 6][s; 51] & + [s; 6][s; 431] & + [s; 6][s; 42^2] \\
+ 4[s; 6][s; 421] & + 4[s; 6][s; 42] & - [s; 6][s; 41^2]\# & + 10[s; 6][s; 41^2] \\
+ 8[s; 6][s; 41] & + 4[s; 6][s; 4] & + 2[s; 6][s; 3^21] & + 2[s; 6][s; 3^2] \\
+ 2[s; 6][s; 32^2] & - [s; 6][s; 321]\# & + 14[s; 6][s; 321] & + 11[s; 6][s; 32] \\
- 4[s; 6][s; 31^2]\# & + 26[s; 6][s; 31^2] & + 25[s; 6][s; 31] & + 11[s; 6][s; 3] \\
+ 4[s; 6][s; 2^3] & - 3[s; 6][s; 2^21]\# & + 20[s; 6][s; 2^21] & + 18[s; 6][s; 2^2] \\
- 7[s; 6][s; 21^2]\# & + 41[s; 6][s; 21^2] & - [s; 6][s; 21]\# & + 40[s; 6][s; 21] \\
+ 21[s; 6][s; 2] & - 7[s; 6][s; 1^3]\# & + 32[s; 6][s; 1^3] & - [s; 6][s; 1^2]\# \\
+ 32[s; 6][s; 1^2] & + 19[s; 6][s; 1] & + 6[s; 6][s; 0] & + [s; 5^2][s; 31] \\
+ [s; 5^2][s; 3] & + [s; 5^2][s; 21^2] & + 2[s; 5^2][s; 21] & + 3[s; 5^2][s; 2] \\
+ [s; 5^2][s; 1^3] & + 3[s; 5^2][s; 1^2] & + 4[s; 5^2][s; 1] & + 2[s; 5^2][s; 0] \\
+ [s; 54][s; 5] & + 3[s; 54][s; 41] & + 4[s; 54][s; 4] & + 3[s; 54][s; 32] \\
+ 4[s; 54][s; 31^2] & + 11[s; 54][s; 31] & + 14[s; 54][s; 3] & + 3[s; 54][s; 2^21] \\
+ 7[s; 54][s; 2^2] & + 10[s; 54][s; 21^2] & + 26[s; 54][s; 21] & + 27[s; 54][s; 2]
\end{array}$$

$$\begin{aligned}
& + 12[s; 54][s; 1^3] & + 26[s; 54][s; 1^2] & + 31[s; 54][s; 1] & + 16[s; 54][s; 0] \\
& - [s; 53]\#[s; 4] & - 2[s; 53]\#[s; 31] & - 3[s; 53]\#[s; 3] & - 2[s; 53]\#[s; 2^2] \\
& - 2[s; 53]\#[s; 21^2] & - 6[s; 53]\#[s; 21] & - 9[s; 53]\#[s; 2] & - 3[s; 53]\#[s; 1^3] \\
& - 9[s; 53]\#[s; 1^2] & - 12[s; 53]\#[s; 1] & - 8[s; 53]\#[s; 0] & + [s; 53][s; 6] \\
& + 3[s; 53][s; 51] & + 4[s; 53][s; 5] & + 6[s; 53][s; 42] & + 6[s; 53][s; 41^2] \\
& + 16[s; 53][s; 41] & + 20[s; 53][s; 4] & + 2[s; 53][s; 3^2] & + 9[s; 53][s; 321] \\
& + 19[s; 53][s; 32] & + 23[s; 53][s; 31^2] & + 58[s; 53][s; 31] & + 54[s; 53][s; 3] \\
& + 3[s; 53][s; 2^3] & + 18[s; 53][s; 2^21] & + 37[s; 53][s; 2^2] & - 2[s; 53][s; 21^2]\# \\
& + 55[s; 53][s; 21^2] & + 105[s; 53][s; 21] & + 101[s; 53][s; 2] & - 3[s; 53][s; 1^3]\# \\
& + 51[s; 53][s; 1^3] & + 97[s; 53][s; 1^2] & + 106[s; 53][s; 1] & + 52[s; 53][s; 0] \\
& - [s; 52]\#[s; 5] & - 3[s; 52]\#[s; 41] & - 3[s; 52]\#[s; 4] & - 4[s; 52]\#[s; 32] \\
& - 4[s; 52]\#[s; 31^2] & - 9[s; 52]\#[s; 31] & - 12[s; 52]\#[s; 3] & - 4[s; 52]\#[s; 2^21] \\
& - 6[s; 52]\#[s; 2^2] & - 9[s; 52]\#[s; 21^2] & - 24[s; 52]\#[s; 21] & - 21[s; 52]\#[s; 2] \\
& + [s; 52]\#[s; 1^3]\# & - 12[s; 52]\#[s; 1^3] & - 21[s; 52]\#[s; 1^2] & - 26[s; 52]\#[s; 1] \\
& - 12[s; 52]\#[s; 0] & + [s; 52][s; 61] & + [s; 52][s; 6] & + 3[s; 52][s; 52] \\
& + 4[s; 52][s; 51^2] & + 8[s; 52][s; 51] & + 10[s; 52][s; 5] & + 3[s; 52][s; 43] \\
& + 10[s; 52][s; 421] & + 16[s; 52][s; 42] & + 21[s; 52][s; 41^2] & + 48[s; 52][s; 41] \\
& + 39[s; 52][s; 4] & + 5[s; 52][s; 3^21] & + 9[s; 52][s; 3^2] & + 6[s; 52][s; 32^2] \\
& + 34[s; 52][s; 321] & + 62[s; 52][s; 32] & - 6[s; 52][s; 31^2]\# & + 83[s; 52][s; 31^2] \\
& + 131[s; 52][s; 31] & + 110[s; 52][s; 3] & + 11[s; 52][s; 2^3] & - 4[s; 52][s; 2^21]\# \\
& + 69[s; 52][s; 2^21] & + 90[s; 52][s; 2^2] & - 14[s; 52][s; 21^2]\# & + 147[s; 52][s; 21^2]\# \\
& - 2[s; 52][s; 21]\# & + 235[s; 52][s; 21] & + 181[s; 52][s; 2] & - 17[s; 52][s; 1^3]\# \\
& + 127[s; 52][s; 1^3] & - 3[s; 52][s; 1^2]\# & + 191[s; 52][s; 1^2] & + 183[s; 52][s; 1] \\
& + 80[s; 52][s; 0] & - [s; 51]\#[s; 51] & - 2[s; 51]\#[s; 42] & - 3[s; 51]\#[s; 41^2] \\
& - 3[s; 51]\#[s; 41] & - 3[s; 51]\#[s; 4] & - 2[s; 51]\#[s; 3^2] & - 6[s; 51]\#[s; 321] \\
& - 6[s; 51]\#[s; 32] & - 9[s; 51]\#[s; 31^2] & - 18[s; 51]\#[s; 31] & - 9[s; 51]\#[s; 3] \\
& - 2[s; 51]\#[s; 2^3] & - 9[s; 51]\#[s; 2^21] & - 15[s; 51]\#[s; 2^2] & + 3[s; 51]\#[s; 21^2]\# \\
& - 27[s; 51]\#[s; 21^2] & - 30[s; 51]\#[s; 21] & - 22[s; 51]\#[s; 2] & + 3[s; 51]\#[s; 1^3]\# \\
& - 21[s; 51]\#[s; 1^3] & + [s; 51]\#[s; 1^2]\# & - 31[s; 51]\#[s; 1^2] & - 21[s; 51]\#[s; 1] \\
& - 9[s; 51]\#[s; 0] & + [s; 51][s; 61^2] & + [s; 51][s; 61] & + [s; 51][s; 6] \\
& + [s; 51][s; 53] & + 4[s; 51][s; 521] & + 4[s; 51][s; 52] & + 8[s; 51][s; 51^2] \\
& + 14[s; 51][s; 51] & + 8[s; 51][s; 5] & + 4[s; 51][s; 431] & + 4[s; 51][s; 43] \\
& + 4[s; 51][s; 42^2] & + 21[s; 51][s; 421] & + 32[s; 51][s; 42] & - 3[s; 51][s; 41^2]\# \\
& + 49[s; 51][s; 41^2] & + 60[s; 51][s; 41] & + 42[s; 51][s; 4] & + 3[s; 51][s; 3^22] \\
& + 12[s; 51][s; 3^21] & + 18[s; 51][s; 3^2] & + 15[s; 51][s; 32^2] & - 5[s; 51][s; 321]\# \\
& + 84[s; 51][s; 321] & + 89[s; 51][s; 32] & - 15[s; 51][s; 31^2]\# & + 138[s; 51][s; 31^2] \\
& - [s; 51][s; 31]\# & + 184[s; 51][s; 31] & + 112[s; 51][s; 3] & - 2[s; 51][s; 2^3]\# \\
& + 30[s; 51][s; 2^3] & - 14[s; 51][s; 2^21]\# & + 124[s; 51][s; 2^21] & - [s; 51][s; 2^2]\# \\
& + 136[s; 51][s; 2^2] & - 36[s; 51][s; 21^2]\# & + 247[s; 51][s; 21^2] & - 6[s; 51][s; 21]\# \\
& + 294[s; 51][s; 21] & + 196[s; 51][s; 2] & - 35[s; 51][s; 1^3]\# & + 186[s; 51][s; 1^3] \\
& - 7[s; 51][s; 1^2]\# & + 234[s; 51][s; 1^2] & - [s; 51][s; 1]\# & + 182[s; 51][s; 1] \\
& + 72[s; 51][s; 0] & + [s; 5][s; 61^2] & + [s; 5][s; 61] & + [s; 5][s; 531] \\
& + [s; 5][s; 52^2] & + 4[s; 5][s; 521] & + 4[s; 5][s; 52] & + 9[s; 5][s; 51^2] \\
& + 8[s; 5][s; 51] & + 4[s; 5][s; 5] & + [s; 5][s; 432] & + 4[s; 5][s; 431] \\
& + 4[s; 5][s; 43] & + 5[s; 5][s; 42^2] & - [s; 5][s; 421]\# & + 25[s; 5][s; 421] \\
& + 21[s; 5][s; 42] & - 3[s; 5][s; 41^2]\# & + 39[s; 5][s; 41^2] & + 43[s; 5][s; 41] \\
& + 21[s; 5][s; 4] & + 3[s; 5][s; 3^22] & + 14[s; 5][s; 3^21] & + 12[s; 5][s; 3^2] \\
& - [s; 5][s; 32^2]\# & + 19[s; 5][s; 32^2] & - 6[s; 5][s; 321]\# & + 70[s; 5][s; 321] \\
& + 67[s; 5][s; 32] & - 18[s; 5][s; 31^2]\# & + 116[s; 5][s; 31^2] & - [s; 5][s; 31]\# \\
& + 115[s; 5][s; 31] & + 64[s; 5][s; 3] & - 3[s; 5][s; 2^3]\# & + 27[s; 5][s; 2^3]
\end{aligned}$$

$$\begin{aligned}
& - 17[s; 5][s; 2^2 1] \# & + 105[s; 5][s; 2^2 1] & - [s; 5][s; 2^2] \# & + 91[s; 5][s; 2^2] \\
& - 35[s; 5][s; 21^2] \# & + 180[s; 5][s; 21^2] & - 7[s; 5][s; 21] \# & + 191[s; 5][s; 21] \\
& + 106[s; 5][s; 2] & - 33[s; 5][s; 1^3] \# & + 134[s; 5][s; 1^3] & - 7[s; 5][s; 1^2] \# \\
& + 140[s; 5][s; 1^2] & - [s; 5][s; 1] \# & + 97[s; 5][s; 1] & + 35[s; 5][s; 0] \\
& - 2[s; 4^2] \# [s; 31] & - 2[s; 4^2] \# [s; 3] & - [s; 4^2] \# [s; 2^2] & - 3[s; 4^2] \# [s; 21^2] \\
& - 6[s; 4^2] \# [s; 21] & - 8[s; 4^2] \# [s; 2] & - 4[s; 4^2] \# [s; 1^3] & - 10[s; 4^2] \# [s; 1^2] \\
& - 12[s; 4^2] \# [s; 1] & - 7[s; 4^2] \# [s; 0] & + 2[s; 4^2][s; 51] & + 2[s; 4^2][s; 5] \\
& + 2[s; 4^2][s; 42] & + 4[s; 4^2][s; 41^2] & + 9[s; 4^2][s; 41] & + 11[s; 4^2][s; 4] \\
& + 2[s; 4^2][s; 3^2] & + 5[s; 4^2][s; 321] & + 11[s; 4^2][s; 32] & + 14[s; 4^2][s; 31^2] \\
& + 35[s; 4^2][s; 31] & + 33[s; 4^2][s; 3] & + [s; 4^2][s; 2^3] & + 11[s; 4^2][s; 2^2 1] \\
& + 23[s; 4^2][s; 2^2] & - [s; 4^2][s; 21^2] \# & + 36[s; 4^2][s; 21^2] & + 68[s; 4^2][s; 21] \\
& + 64[s; 4^2][s; 2] & - 2[s; 4^2][s; 1^3] \# & + 35[s; 4^2][s; 1^3] & + 68[s; 4^2][s; 1^2] \\
& + 72[s; 4^2][s; 1] & + 36[s; 4^2][s; 0] & - [s; 43] \# [s; 5] & - 5[s; 43] \# [s; 41] \\
& - 6[s; 43] \# [s; 4] & - 7[s; 43] \# [s; 32] & - 9[s; 43] \# [s; 31^2] & - 21[s; 43] \# [s; 31] \\
& - 26[s; 43] \# [s; 3] & - 8[s; 43] \# [s; 2^2 1] & - 15[s; 43] \# [s; 2^2] & - 24[s; 43] \# [s; 21^2] \\
& - 57[s; 43] \# [s; 21] & - 54[s; 43] \# [s; 2] & + 2[s; 43] \# [s; 1^3] \# & - 31[s; 43] \# [s; 1^3] \\
& - 57[s; 43] \# [s; 1^2] & - 66[s; 43] \# [s; 1] & - 33[s; 43] \# [s; 0] & + [s; 43][s; 61] \\
& + [s; 43][s; 6] & + 3[s; 43][s; 52] & + 4[s; 43][s; 51^2] & + 9[s; 43][s; 51] \\
& + 12[s; 43][s; 5] & + 3[s; 43][s; 43] & + 10[s; 43][s; 421] & + 19[s; 43][s; 42] \\
& + 24[s; 43][s; 41^2] & + 59[s; 43][s; 41] & + 53[s; 43][s; 4] & + 6[s; 43][s; 3^2 1] \\
& + 11[s; 43][s; 3^2] & + 6[s; 43][s; 32^2] & + 39[s; 43][s; 321] & + 78[s; 43][s; 32] \\
& - 5[s; 43][s; 31^2] \# & + 100[s; 43][s; 31^2] & + 176[s; 43][s; 31] & + 154[s; 43][s; 3] \\
& + 12[s; 43][s; 2^3] & - 4[s; 43][s; 2^2 1] \# & + 83[s; 43][s; 2^2 1] & + 120[s; 43][s; 2^2] \\
& - 13[s; 43][s; 21^2] \# & + 188[s; 43][s; 21^2] & - [s; 43][s; 21] \# & + 324[s; 43][s; 21] \\
& + 266[s; 43][s; 2] & - 17[s; 43][s; 1^3] \# & + 169[s; 43][s; 1^3] & - 2[s; 43][s; 1^2] \# \\
& + 274[s; 43][s; 1^2] & + 275[s; 43][s; 1] & + 125[s; 43][s; 0] & - [s; 42] \# [s; 6] \\
& - 4[s; 42] \# [s; 51] & - 4[s; 42] \# [s; 5] & - 9[s; 42] \# [s; 42] & - 9[s; 42] \# [s; 41^2] \\
& - 19[s; 42] \# [s; 41] & - 22[s; 42] \# [s; 4] & - 5[s; 42] \# [s; 3^2] & - 18[s; 42] \# [s; 321] \\
& - 28[s; 42] \# [s; 32] & - 35[s; 42] \# [s; 31^2] & - 78[s; 42] \# [s; 31] & - 61[s; 42] \# [s; 3] \\
& - 7[s; 42] \# [s; 2^3] & - 33[s; 42] \# [s; 2^2 1] & - 58[s; 42] \# [s; 2^2] & + 8[s; 42] \# [s; 21^2] \# \\
& - 92[s; 42] \# [s; 21^2] & - 141[s; 42] \# [s; 21] & - 121[s; 42] \# [s; 2] & + 9[s; 42] \# [s; 1^3] \# \\
& - 80[s; 42] \# [s; 1^3] & + 2[s; 42] \# [s; 1^2] \# & - 131[s; 42] \# [s; 1^2] & - 124[s; 42] \# [s; 1] \\
& - 58[s; 42] \# [s; 0] & + [s; 42][s; 62] & + [s; 42][s; 61^2] & + 2[s; 42][s; 61] \\
& + 4[s; 42][s; 6] & + [s; 42][s; 53] & + 6[s; 42][s; 521] & + 9[s; 42][s; 52] \\
& + 13[s; 42][s; 51^2] & + 32[s; 42][s; 51] & + 26[s; 42][s; 5] & + [s; 42][s; 4^2] \\
& + 7[s; 42][s; 431] & + 11[s; 42][s; 43] & + 8[s; 42][s; 42^2] & + 39[s; 42][s; 421] \\
& + 73[s; 42][s; 42] & - 5[s; 42][s; 41^2] \# & + 92[s; 42][s; 41^2] & + 145[s; 42][s; 41] \\
& + 120[s; 42][s; 4] & + 5[s; 42][s; 3^2 2] & + 25[s; 42][s; 3^2 1] & + 44[s; 42][s; 3^2] \\
& + 29[s; 42][s; 32^2] & - 9[s; 42][s; 321] \# & + 168[s; 42][s; 321] & + 211[s; 42][s; 32] \\
& - 22[s; 42][s; 31^2] \# & + 279[s; 42][s; 31^2] & - 2[s; 42][s; 31] \# & + 434[s; 42][s; 31] \\
& + 307[s; 42][s; 3] & - 4[s; 42][s; 2^3] \# & + 60[s; 42][s; 2^3] & - 22[s; 42][s; 2^2 1] \# \\
& + 253[s; 42][s; 2^2 1] & - 2[s; 42][s; 2^2] \# & + 318[s; 42][s; 2^2] & - 60[s; 42][s; 21^2] \# \\
& + 506[s; 42][s; 21^2] & - 8[s; 42][s; 21] \# & + 701[s; 42][s; 21] & + 519[s; 42][s; 2] \\
& - 56[s; 42][s; 1^3] \# & + 388[s; 42][s; 1^3] & - 11[s; 42][s; 1^2] \# & + 560[s; 42][s; 1^2] \\
& - [s; 42][s; 1] \# & + 492[s; 42][s; 1] & + 211[s; 42][s; 0] & - [s; 41] \# [s; 61] \\
& - 3[s; 41] \# [s; 52] & - 3[s; 41] \# [s; 51^2] & - 4[s; 41] \# [s; 51] & - 4[s; 41] \# [s; 5] \\
& - 4[s; 41] \# [s; 43] & - 10[s; 41] \# [s; 421] & - 13[s; 41] \# [s; 42] & - 15[s; 41] \# [s; 41^2] \\
& - 31[s; 41] \# [s; 41] & - 19[s; 41] \# [s; 4] & - 7[s; 41] \# [s; 3^2 1] & - 9[s; 41] \# [s; 3^2] \\
& - 8[s; 41] \# [s; 32^2] & - 34[s; 41] \# [s; 321] & - 53[s; 41] \# [s; 32] & + 6[s; 41] \# [s; 31^2] \# \\
& - 68[s; 41] \# [s; 31^2] & - 91[s; 41] \# [s; 31] & - 65[s; 41] \# [s; 3] & - 14[s; 41] \# [s; 2^3]
\end{aligned}$$

$$\begin{aligned}
& + 7[s; 41]\#[s; 2^2 1]\# & - 69[s; 41]\#[s; 2^2 1] & - 75[s; 41]\#[s; 2^2] & + 17[s; 41]\#[s; 21^2]\# \\
& - 124[s; 41]\#[s; 21^2] & + 4[s; 41]\#[s; 21]\# & - 171[s; 41]\#[s; 21] & - 114[s; 41]\#[s; 2] \\
& + 20[s; 41]\#[s; 1^3]\# & - 103[s; 41]\#[s; 1^3] & + 5[s; 41]\#[s; 1^2]\# & - 134[s; 41]\#[s; 1^2] \\
& + [s; 41]\#[s; 1]\# & - 114[s; 41]\#[s; 1] & - 47[s; 41]\#[s; 0] & + [s; 41][s; 621] \\
& + [s; 41][s; 62] & + 2[s; 41][s; 61^2] & + 5[s; 41][s; 61] & + 2[s; 41][s; 6] \\
& + 2[s; 41][s; 531] & + 2[s; 41][s; 53] & + 3[s; 41][s; 52^2] & + 13[s; 41][s; 521] \\
& + 22[s; 41][s; 52] & + 30[s; 41][s; 51^2] & + 39[s; 41][s; 51] & + 29[s; 41][s; 5] \\
& + [s; 41][s; 4^2 1] & + [s; 41][s; 4^2] & + 4[s; 41][s; 432] & + 16[s; 41][s; 431] \\
& + 26[s; 41][s; 43] & + 20[s; 41][s; 42^2] & - 3[s; 41][s; 421]\# & + 99[s; 41][s; 421] \\
& + 108[s; 41][s; 42] & - 9[s; 41][s; 41^2]\# & + 146[s; 41][s; 41^2] & + 206[s; 41][s; 41] \\
& + 126[s; 41][s; 4] & + [s; 41][s; 3^3] & + 15[s; 41][s; 3^2 2] & - 2[s; 41][s; 3^2 1]\# \\
& + 64[s; 41][s; 3^2 1] & + 68[s; 41][s; 3^2] & - 5[s; 41][s; 32^2]\# & + 83[s; 41][s; 32^2] \\
& - 23[s; 41][s; 321]\# & + 297[s; 41][s; 321] & - [s; 41][s; 32]\# & + 331[s; 41][s; 32] \\
& - 56[s; 41][s; 31^2]\# & + 457[s; 41][s; 31^2] & - 5[s; 41][s; 31]\# & + 553[s; 41][s; 31] \\
& + 350[s; 41][s; 3] & - 14[s; 41][s; 2^3]\# & + 120[s; 41][s; 2^3] & - 62[s; 41][s; 2^2 1]\# \\
& + 444[s; 41][s; 2^2 1] & - 6[s; 41][s; 2^2]\# & + 435[s; 41][s; 2^2] & - 121[s; 41][s; 21^2]\# \\
& + 733[s; 41][s; 21^2] & - 24[s; 41][s; 21]\# & + 892[s; 41][s; 21] & - [s; 41][s; 2]\# \\
& + 562[s; 41][s; 2] & - 110[s; 41][s; 1^3]\# & + 534[s; 41][s; 1^3] & - 25[s; 41][s; 1^2]\# \\
& + 650[s; 41][s; 1^2] & - 4[s; 41][s; 1]\# & + 515[s; 41][s; 1] & + 200[s; 41][s; 0] \\
& - [s; 4]\#[s; 42] & - [s; 4]\#[s; 41^2] & - [s; 4]\#[s; 41] & - [s; 4]\#[s; 4] \\
& - [s; 4]\#[s; 3^2] & - 4[s; 4]\#[s; 321] & - 4[s; 4]\#[s; 32] & - 5[s; 4]\#[s; 31^2] \\
& - 10[s; 4]\#[s; 31] & - 5[s; 4]\#[s; 3] & - 2[s; 4]\#[s; 2^3] & - 7[s; 4]\#[s; 2^2 1] \\
& - 11[s; 4]\#[s; 2^2] & + 3[s; 4]\#[s; 21^2]\# & - 19[s; 4]\#[s; 21^2] & - 20[s; 4]\#[s; 21] \\
& - 15[s; 4]\#[s; 2] & + 3[s; 4]\#[s; 1^3]\# & - 15[s; 4]\#[s; 1^3] & + [s; 4]\#[s; 1^2]\# \\
& - 21[s; 4]\#[s; 1^2] & - 15[s; 4]\#[s; 1] & - 7[s; 4]\#[s; 0] & + [s; 4][s; 621] \\
& + [s; 4][s; 62] & + 3[s; 4][s; 61^2] & + 2[s; 4][s; 61] & + [s; 4][s; 6] \\
& + [s; 4][s; 532] & + 2[s; 4][s; 531] & + 2[s; 4][s; 53] & + 4[s; 4][s; 52^2] \\
& + 16[s; 4][s; 521] & + 13[s; 4][s; 52] & + 22[s; 4][s; 51^2] & + 27[s; 4][s; 51] \\
& + 13[s; 4][s; 5] & + [s; 4][s; 4^2 1] & + [s; 4][s; 4^2] & + 5[s; 4][s; 432] \\
& + 19[s; 4][s; 431] & + 16[s; 4][s; 43] & - [s; 4][s; 42^2]\# & + 25[s; 4][s; 42^2] \\
& - 3[s; 4][s; 421]\# & + 79[s; 4][s; 421] & + 79[s; 4][s; 42] & - 12[s; 4][s; 41^2]\# \\
& + 118[s; 4][s; 41^2] & + 123[s; 4][s; 41] & + 69[s; 4][s; 4] & + [s; 4][s; 3^3] \\
& + 18[s; 4][s; 3^2 2] & - 2[s; 4][s; 3^2 1]\# & + 51[s; 4][s; 3^2 1] & + 51[s; 4][s; 3^2] \\
& - 6[s; 4][s; 32^2]\# & + 73[s; 4][s; 32^2] & - 28[s; 4][s; 321]\# & + 244[s; 4][s; 321] \\
& - [s; 4][s; 32]\# & + 216[s; 4][s; 32] & - 49[s; 4][s; 31^2]\# & + 318[s; 4][s; 31^2] \\
& - 6[s; 4][s; 31]\# & + 349[s; 4][s; 31] & + 188[s; 4][s; 3] & - 17[s; 4][s; 2^3]\# \\
& + 102[s; 4][s; 2^3] & - 55[s; 4][s; 2^2 1]\# & + 322[s; 4][s; 2^2 1] & - 7[s; 4][s; 2^2]\# \\
& + 289[s; 4][s; 2^2] & - 100[s; 4][s; 21^2]\# & + 505[s; 4][s; 21^2] & - 20[s; 4][s; 21]\# \\
& + 533[s; 4][s; 21] & - [s; 4][s; 2]\# & + 307[s; 4][s; 2] & - 81[s; 4][s; 1^3]\# \\
& + 340[s; 4][s; 1^3] & - 19[s; 4][s; 1^2]\# & + 379[s; 4][s; 1^2] & - 3[s; 4][s; 1]\# \\
& + 268[s; 4][s; 1] & + 98[s; 4][s; 0] & - 3[s; 3^2]\#[s; 51] & - 3[s; 3^2]\#[s; 5] \\
& - 5[s; 3^2]\#[s; 42] & - 8[s; 3^2]\#[s; 41^2] & - 16[s; 3^2]\#[s; 41] & - 19[s; 3^2]\#[s; 4] \\
& - 4[s; 3^2]\#[s; 3^2] & - 12[s; 3^2]\#[s; 321] & - 21[s; 3^2]\#[s; 32] & - 28[s; 3^2]\#[s; 31^2] \\
& - 64[s; 3^2]\#[s; 31] & - 55[s; 3^2]\#[s; 3] & - 3[s; 3^2]\#[s; 2^3] & - 23[s; 3^2]\#[s; 2^2 1] \\
& - 43[s; 3^2]\#[s; 2^2] & + 4[s; 3^2]\#[s; 21^2]\# & - 70[s; 3^2]\#[s; 21^2] & - 117[s; 3^2]\#[s; 21] \\
& - 104[s; 3^2]\#[s; 2] & + 5[s; 3^2]\#[s; 1^3]\# & - 62[s; 3^2]\#[s; 1^3] & + [s; 3^2]\#[s; 1^2]\# \\
& - 111[s; 3^2]\#[s; 1^2] & - 110[s; 3^2]\#[s; 1] & - 52[s; 3^2]\#[s; 0] & + [s; 3^2][s; 61^2] \\
& + [s; 3^2][s; 61] & + 2[s; 3^2][s; 6] & + [s; 3^2][s; 53] & + 3[s; 3^2][s; 521] \\
& + 5[s; 3^2][s; 52] & + 7[s; 3^2][s; 51^2] & + 19[s; 3^2][s; 51] & + 17[s; 3^2][s; 5] \\
& + 4[s; 3^2][s; 431] & + 7[s; 3^2][s; 43] & + 3[s; 3^2][s; 42^2] & + 22[s; 3^2][s; 421]
\end{aligned}$$

$$\begin{aligned}
& + 44[s; 3^2][s; 42] & - 2[s; 3^2][s; 41^2]\# & + 55[s; 3^2][s; 41^2] & + 93[s; 3^2][s; 41] \\
& + 79[s; 3^2][s; 4] & + 4[s; 3^2][s; 3^2] & + 15[s; 3^2][s; 3^2 1] & + 27[s; 3^2][s; 3^2] \\
& + 16[s; 3^2][s; 32^2] & - 5[s; 3^2][s; 321]\# & + 98[s; 3^2][s; 321] & + 132[s; 3^2][s; 32] \\
& - 11[s; 3^2][s; 31^2]\# & + 169[s; 3^2][s; 31^2] & - [s; 3^2][s; 31]\# & + 282[s; 3^2][s; 31] \\
& + 209[s; 3^2][s; 3] & - 3[s; 3^2][s; 2^3]\# & + 33[s; 3^2][s; 2^3] & - 11[s; 3^2][s; 2^2 1]\# \\
& + 148[s; 3^2][s; 2^2 1] & - [s; 3^2][s; 2^2]\# & + 194[s; 3^2][s; 2^2] & - 30[s; 3^2][s; 21^2]\# \\
& + 309[s; 3^2][s; 21^2] & - 3[s; 3^2][s; 21]\# & + 453[s; 3^2][s; 21] & + 351[s; 3^2][s; 2] \\
& - 27[s; 3^2][s; 1^3]\# & + 237[s; 3^2][s; 1^3] & - 4[s; 3^2][s; 1^2]\# & + 365[s; 3^2][s; 1^2] \\
& + 336[s; 3^2][s; 1] & + 145[s; 3^2][s; 0] & - [s; 32]\#[s; 61] & - [s; 32]\#[s; 6] \\
& - 5[s; 32]\#[s; 52] & - 5[s; 32]\#[s; 51^2] & - 11[s; 32]\#[s; 51] & - 12[s; 32]\#[s; 5] \\
& - 7[s; 32]\#[s; 43] & - 18[s; 32]\#[s; 421] & - 29[s; 32]\#[s; 42] & - 32[s; 32]\#[s; 41^2] \\
& - 71[s; 32]\#[s; 41] & - 54[s; 32]\#[s; 4] & - 13[s; 32]\#[s; 3^2 1] & - 19[s; 32]\#[s; 3^2] \\
& - 13[s; 32]\#[s; 32^2] & - 63[s; 32]\#[s; 321] & - 109[s; 32]\#[s; 32] & + 9[s; 32]\#[s; 31^2]\# \\
& - 132[s; 32]\#[s; 31^2] & - 202[s; 32]\#[s; 31] & - 157[s; 32]\#[s; 3] & - 22[s; 32]\#[s; 2^3] \\
& + 10[s; 32]\#[s; 2^2 1]\# & - 122[s; 32]\#[s; 2^2 1] & - 149[s; 32]\#[s; 2^2] & + 21[s; 32]\#[s; 21^2]\# \\
& - 225[s; 32]\#[s; 21^2] & + 4[s; 32]\#[s; 21]\# & - 353[s; 32]\#[s; 21] & - 258[s; 32]\#[s; 2] \\
& + 24[s; 32]\#[s; 1^3]\# & - 185[s; 32]\#[s; 1^3] & + 4[s; 32]\#[s; 1^2]\# & - 271[s; 32]\#[s; 1^2] \\
& + [s; 32]\#[s; 1]\# & - 252[s; 32]\#[s; 1] & - 107[s; 32]\#[s; 0] & + [s; 32][s; 621] \\
& + [s; 32][s; 62] & + 2[s; 32][s; 61^2] & + 6[s; 32][s; 61] & + 5[s; 32][s; 6] \\
& + 2[s; 32][s; 531] & + 3[s; 32][s; 53] & + 3[s; 32][s; 52^2] & + 14[s; 32][s; 521] \\
& + 29[s; 32][s; 52] & + 35[s; 32][s; 51^2] & + 58[s; 32][s; 51] & + 48[s; 32][s; 5] \\
& + [s; 32][s; 4^2 1] & + 2[s; 32][s; 4^2] & + 5[s; 32][s; 432] & + 21[s; 32][s; 431] \\
& + 39[s; 32][s; 43] & + 23[s; 32][s; 42^2] & - 4[s; 32][s; 421]\# & + 124[s; 32][s; 421] \\
& + 156[s; 32][s; 42] & - 9[s; 32][s; 41^2]\# & + 187[s; 32][s; 41^2] & + 299[s; 32][s; 41] \\
& + 204[s; 32][s; 4] & + 2[s; 32][s; 3^3] & + 20[s; 32][s; 3^2 2] & - 3[s; 32][s; 3^2 1]\# \\
& + 87[s; 32][s; 3^2 1] & + 102[s; 32][s; 3^2] & - 7[s; 32][s; 32^2]\# & + 104[s; 32][s; 32^2] \\
& - 28[s; 32][s; 321]\# & + 384[s; 32][s; 321] & - 2[s; 32][s; 32]\# & + 468[s; 32][s; 32] \\
& - 59[s; 32][s; 31^2]\# & + 590[s; 32][s; 31^2] & - 5[s; 32][s; 31]\# & + 792[s; 32][s; 31] \\
& + 537[s; 32][s; 3] & - 18[s; 32][s; 2^3]\# & + 148[s; 32][s; 2^3] & - 69[s; 32][s; 2^2 1]\# \\
& + 561[s; 32][s; 2^2 1] & - 8[s; 32][s; 2^2]\# & + 599[s; 32][s; 2^2] & - 124[s; 32][s; 21^2]\# \\
& + 929[s; 32][s; 21^2] & - 21[s; 32][s; 21]\# & + 1242[s; 32][s; 21] & - [s; 32][s; 2]\# \\
& + 837[s; 32][s; 2] & - 105[s; 32][s; 1^3]\# & + 668[s; 32][s; 1^3] & - 20[s; 32][s; 1^2]\# \\
& + 898[s; 32][s; 1^2] & - 2[s; 32][s; 1]\# & + 761[s; 32][s; 1] & + 306[s; 32][s; 0] \\
& - [s; 31]\#[s; 62] & - [s; 31]\#[s; 61] & - [s; 31]\#[s; 6] & - 2[s; 31]\#[s; 53] \\
& - 4[s; 31]\#[s; 52 1] & - 8[s; 31]\#[s; 52] & - 6[s; 31]\#[s; 51^2] & - 15[s; 31]\#[s; 51] \\
& - 11[s; 31]\#[s; 5] & - 2[s; 31]\#[s; 4^2] & - 8[s; 31]\#[s; 431] & - 13[s; 31]\#[s; 43] \\
& - 8[s; 31]\#[s; 42^2] & - 32[s; 31]\#[s; 421] & - 53[s; 31]\#[s; 42] & + 3[s; 31]\#[s; 41^2]\# \\
& - 54[s; 31]\#[s; 41^2] & - 82[s; 31]\#[s; 41] & - 59[s; 31]\#[s; 4] & - 7[s; 31]\#[s; 3^2 2] \\
& - 26[s; 31]\#[s; 3^2 1] & - 39[s; 31]\#[s; 3^2] & - 30[s; 31]\#[s; 32^2] & + 10[s; 31]\#[s; 321]\# \\
& - 134[s; 31]\#[s; 321] & - 151[s; 31]\#[s; 32] & + 17[s; 31]\#[s; 31^2]\# & - 178[s; 31]\#[s; 31^2] \\
& + 3[s; 31]\#[s; 31]\# & - 256[s; 31]\#[s; 31] & - 160[s; 31]\#[s; 3] & + 6[s; 31]\#[s; 2^3]\# \\
& - 55[s; 31]\#[s; 2^3] & + 21[s; 31]\#[s; 2^2 1]\# & - 187[s; 31]\#[s; 2^2 1] & + 4[s; 31]\#[s; 2^2]\# \\
& - 213[s; 31]\#[s; 2^2] & + 49[s; 31]\#[s; 21^2]\# & - 320[s; 31]\#[s; 21^2] & + 8[s; 31]\#[s; 21]\# \\
& - 399[s; 31]\#[s; 21] & + [s; 31]\#[s; 2]\# & - 268[s; 31]\#[s; 2] & + 39[s; 31]\#[s; 1^3]\# \\
& - 221[s; 31]\#[s; 1^3] & + 10[s; 31]\#[s; 1^2]\# & - 297[s; 31]\#[s; 1^2] & + [s; 31]\#[s; 1]\# \\
& - 236[s; 31]\#[s; 1] & - 95[s; 31]\#[s; 0] & + [s; 31][s; 62^2] & + 2[s; 31][s; 621] \\
& + 4[s; 31][s; 62] & + 5[s; 31][s; 61^2] & + 7[s; 31][s; 61] & + 6[s; 31][s; 6] \\
& + [s; 31][s; 532] & + 5[s; 31][s; 531] & + 10[s; 31][s; 53] & + 9[s; 31][s; 52^2] \\
& + 40[s; 31][s; 521] & + 46[s; 31][s; 52] & + 55[s; 31][s; 51^2] & + 85[s; 31][s; 51] \\
& + 53[s; 31][s; 5] & + [s; 31][s; 4^2 2] & + 3[s; 31][s; 4^2 1] & + 6[s; 31][s; 4^2]
\end{aligned}$$

$$\begin{aligned}
& + [s; 31][s; 43^2] & + 15[s; 31][s; 432] & + 59[s; 31][s; 431] & + 66[s; 31][s; 43] \\
& - 2[s; 31][s; 42^2]\# & + 71[s; 31][s; 42^2] & - 9[s; 31][s; 421]\# & + 230[s; 31][s; 421] \\
& + 266[s; 31][s; 42] & - 27[s; 31][s; 41^2]\# & + 320[s; 31][s; 41^2] & + 399[s; 31][s; 41] \\
& + 248[s; 31][s; 4] & + 5[s; 31][s; 3^3] & - 2[s; 31][s; 3^22]\# & + 61[s; 31][s; 3^22] \\
& - 8[s; 31][s; 3^21]\# & + 168[s; 31][s; 3^21] & + 179[s; 31][s; 3^2] & - 21[s; 31][s; 32^2]\# \\
& + 222[s; 31][s; 32^2] & - 80[s; 31][s; 321]\# & + 725[s; 31][s; 321] & - 5[s; 31][s; 32]\# \\
& + 702[s; 31][s; 32] & - 116[s; 31][s; 31^2]\# & + 899[s; 31][s; 31^2] & - 17[s; 31][s; 31]\# \\
& + 1096[s; 31][s; 31] & + 634[s; 31][s; 3] & - 54[s; 31][s; 2^3]\# & + 309[s; 31][s; 2^3] \\
& - 147[s; 31][s; 2^21]\# & + 929[s; 31][s; 2^21] & - 24[s; 31][s; 2^2]\# & + 891[s; 31][s; 2^2] \\
& - 247[s; 31][s; 21^2]\# & + 1405[s; 31][s; 21^2] & - 45[s; 31][s; 21]\# & + 1610[s; 31][s; 21] \\
& - 4[s; 31][s; 2]\# & + 991[s; 31][s; 2] & - 180[s; 31][s; 1^3]\# & + 912[s; 31][s; 1^3] \\
& - 41[s; 31][s; 1^2]\# & + 1111[s; 31][s; 1^2] & - 5[s; 31][s; 1]\# & + 840[s; 31][s; 1] \\
& + 316[s; 31][s; 0] & - [s; 3]\#[s; 52] & - [s; 3]\#[s; 51^2] & - [s; 3]\#[s; 51] \\
& - [s; 3]\#[s; 5] & - 2[s; 3]\#[s; 43] & - 5[s; 3]\#[s; 421] & - 6[s; 3]\#[s; 42] \\
& - 6[s; 3]\#[s; 41^2] & - 13[s; 3]\#[s; 41] & - 7[s; 3]\#[s; 4] & - 4[s; 3]\#[s; 3^21] \\
& - 5[s; 3]\#[s; 3^2] & - 5[s; 3]\#[s; 32^2] & - 17[s; 3]\#[s; 321] & - 27[s; 3]\#[s; 32] \\
& + 4[s; 3]\#[s; 31^2]\# & - 32[s; 3]\#[s; 31^2] & - 39[s; 3]\#[s; 31] & - 27[s; 3]\#[s; 3] \\
& - 7[s; 3]\#[s; 2^3] & + 4[s; 3]\#[s; 2^21]\# & - 34[s; 3]\#[s; 2^21] & - 34[s; 3]\#[s; 2^2] \\
& + 8[s; 3]\#[s; 21^2]\# & - 53[s; 3]\#[s; 21^2] & + 2[s; 3]\#[s; 21]\# & - 72[s; 3]\#[s; 21] \\
& - 44[s; 3]\#[s; 2] & + 9[s; 3]\#[s; 1^3]\# & - 41[s; 3]\#[s; 1^3] & + 2[s; 3]\#[s; 1^2]\# \\
& - 51[s; 3]\#[s; 1^2] & - 42[s; 3]\#[s; 1] & - 16[s; 3]\#[s; 0] & + [s; 3][s; 62^2] \\
& + 3[s; 3][s; 621] & + 2[s; 3][s; 62] & + 4[s; 3][s; 61^2] & + 5[s; 3][s; 61] \\
& + 2[s; 3][s; 6] & + 2[s; 3][s; 532] & + 7[s; 3][s; 531] & + 5[s; 3][s; 53] \\
& + 12[s; 3][s; 52^2] & + 33[s; 3][s; 521] & + 34[s; 3][s; 52] & + 44[s; 3][s; 51^2] \\
& + 50[s; 3][s; 51] & + 28[s; 3][s; 5] & + [s; 3][s; 4^22] & + 4[s; 3][s; 4^21] \\
& + 3[s; 3][s; 4^2] & + [s; 3][s; 43^2] & + 19[s; 3][s; 432] & + 47[s; 3][s; 431] \\
& + 48[s; 3][s; 43] & - 3[s; 3][s; 42^2]\# & + 64[s; 3][s; 42^2] & - 12[s; 3][s; 421]\# \\
& + 192[s; 3][s; 421] & + 172[s; 3][s; 42] & - 21[s; 3][s; 41^2]\# & + 221[s; 3][s; 41^2] \\
& + 252[s; 3][s; 41] & + 131[s; 3][s; 4] & + 6[s; 3][s; 3^3] & - 2[s; 3][s; 3^22]\# \\
& + 53[s; 3][s; 3^22] & - 10[s; 3][s; 3^21]\# & + 137[s; 3][s; 3^21] & + 119[s; 3][s; 3^2] \\
& - 26[s; 3][s; 32^2]\# & + 194[s; 3][s; 32^2] & - 69[s; 3][s; 321]\# & + 526[s; 3][s; 321] \\
& - 6[s; 3][s; 32]\# & + 470[s; 3][s; 32] & - 98[s; 3][s; 31^2]\# & + 624[s; 3][s; 31^2] \\
& - 13[s; 3][s; 31]\# & + 658[s; 3][s; 31] & + 354[s; 3][s; 3] & - 50[s; 3][s; 2^3]\# \\
& + 237[s; 3][s; 2^3] & - 127[s; 3][s; 2^21]\# & + 668[s; 3][s; 2^21] & - 20[s; 3][s; 2^2]\# \\
& + 562[s; 3][s; 2^2] & - 186[s; 3][s; 21^2]\# & + 912[s; 3][s; 21^2] & - 38[s; 3][s; 21]\# \\
& + 968[s; 3][s; 21] & - 3[s; 3][s; 2]\# & + 534[s; 3][s; 2] & - 134[s; 3][s; 1^3]\# \\
& + 573[s; 3][s; 1^3] & - 32[s; 3][s; 1^2]\# & + 631[s; 3][s; 1^2] & - 4[s; 3][s; 1]\# \\
& + 443[s; 3][s; 1] & + 155[s; 3][s; 0] & - [s; 2^2]\#[s; 61] & - 2[s; 2^2]\#[s; 6] \\
& - 2[s; 2^2]\#[s; 53] & - 3[s; 2^2]\#[s; 521] & - 7[s; 2^2]\#[s; 52] & - 6[s; 2^2]\#[s; 51^2] \\
& - 17[s; 2^2]\#[s; 51] & - 14[s; 2^2]\#[s; 5] & - [s; 2^2]\#[s; 4^2] & - 8[s; 2^2]\#[s; 431] \\
& - 13[s; 2^2]\#[s; 43] & - 5[s; 2^2]\#[s; 42^2] & - 29[s; 2^2]\#[s; 421] & - 51[s; 2^2]\#[s; 42] \\
& + 2[s; 2^2]\#[s; 41^2]\# & - 51[s; 2^2]\#[s; 41^2] & - 83[s; 2^2]\#[s; 41] & - 62[s; 2^2]\#[s; 4] \\
& - 7[s; 2^2]\#[s; 3^22] & - 25[s; 2^2]\#[s; 3^21] & - 38[s; 2^2]\#[s; 3^2] & - 25[s; 2^2]\#[s; 32^2] \\
& + 9[s; 2^2]\#[s; 321]\# & - 117[s; 2^2]\#[s; 321] & - 140[s; 2^2]\#[s; 32] & + 12[s; 2^2]\#[s; 31^2]\# \\
& - 154[s; 2^2]\#[s; 31^2] & + 2[s; 2^2]\#[s; 31]\# & - 237[s; 2^2]\#[s; 31] & - 153[s; 2^2]\#[s; 3] \\
& + 6[s; 2^2]\#[s; 2^3]\# & - 43[s; 2^2]\#[s; 2^3] & + 16[s; 2^2]\#[s; 2^21]\# & - 153[s; 2^2]\#[s; 2^21] \\
& + 3[s; 2^2]\#[s; 2^2]\# & - 179[s; 2^2]\#[s; 2^2] & + 31[s; 2^2]\#[s; 21^2]\# & - 256[s; 2^2]\#[s; 21^2] \\
& + 4[s; 2^2]\#[s; 21]\# & - 341[s; 2^2]\#[s; 21] & + [s; 2^2]\#[s; 2]\# & - 235[s; 2^2]\#[s; 2] \\
& + 21[s; 2^2]\#[s; 1^3]\# & - 167[s; 2^2]\#[s; 1^3] & + 4[s; 2^2]\#[s; 1^2]\# & - 242[s; 2^2]\#[s; 1^2] \\
& - 200[s; 2^2]\#[s; 1] & - 78[s; 2^2]\#[s; 0] & + [s; 2^2][s; 621] & + 2[s; 2^2][s; 62]
\end{aligned}$$

$$\begin{aligned}
& + 3[s; 2^2][s; 61^2] & + 5[s; 2^2][s; 61] & + 5[s; 2^2][s; 6] & + [s; 2^2][s; 532] \\
& + 3[s; 2^2][s; 531] & + 7[s; 2^2][s; 53] & + 5[s; 2^2][s; 52^2] & + 24[s; 2^2][s; 521] \\
& + 32[s; 2^2][s; 52] & + 35[s; 2^2][s; 51^2] & + 63[s; 2^2][s; 51] & + 43[s; 2^2][s; 5] \\
& + 2[s; 2^2][s; 4^2 1] & + 5[s; 2^2][s; 4^2] & + [s; 2^2][s; 43^2] & + 10[s; 2^2][s; 432] \\
& + 41[s; 2^2][s; 431] & + 50[s; 2^2][s; 43] & - 2[s; 2^2][s; 42^2]\# & + 44[s; 2^2][s; 42^2] \\
& - 6[s; 2^2][s; 421]\# & + 152[s; 2^2][s; 421] & + 186[s; 2^2][s; 42] & - 15[s; 2^2][s; 41^2]\# \\
& + 213[s; 2^2][s; 41^2] & + 285[s; 2^2][s; 41] & + 186[s; 2^2][s; 4] & + 4[s; 2^2][s; 3^3] \\
& - [s; 2^2][s; 3^2 2]\# & + 42[s; 2^2][s; 3^2 2] & - 6[s; 2^2][s; 3^2 1]\# & + 118[s; 2^2][s; 3^2 1] \\
& + 134[s; 2^2][s; 3^2] & - 15[s; 2^2][s; 32^2]\# & + 146[s; 2^2][s; 32^2] & - 52[s; 2^2][s; 321]\# \\
& + 481[s; 2^2][s; 321] & - 4[s; 2^2][s; 32]\# & + 489[s; 2^2][s; 32] & - 66[s; 2^2][s; 31^2]\# \\
& + 586[s; 2^2][s; 31^2] & - 9[s; 2^2][s; 31]\# & + 756[s; 2^2][s; 31] & + 453[s; 2^2][s; 3] \\
& - 36[s; 2^2][s; 2^3]\# & + 194[s; 2^2][s; 2^3] & - 90[s; 2^2][s; 2^2 1]\# & + 599[s; 2^2][s; 2^2 1] \\
& - 16[s; 2^2][s; 2^2]\# & + 598[s; 2^2][s; 2^2] & - 136[s; 2^2][s; 21^2]\# & + 891[s; 2^2][s; 21^2] \\
& - 22[s; 2^2][s; 21]\# & + 1074[s; 2^2][s; 21] & - 2[s; 2^2][s; 2]\# & + 676[s; 2^2][s; 2] \\
& - 91[s; 2^2][s; 1^3]\# & + 562[s; 2^2][s; 1^3] & - 18[s; 2^2][s; 1^2]\# & + 730[s; 2^2][s; 1^2] \\
& - [s; 2^2][s; 1]\# & + 567[s; 2^2][s; 1] & + 215[s; 2^2][s; 0] & - [s; 21]\#[s; 62] \\
& - 2[s; 21]\#[s; 61] & - [s; 21]\#[s; 6] & - [s; 21]\#[s; 531] & - 4[s; 21]\#[s; 53] \\
& - [s; 21]\#[s; 52^2] & - 7[s; 21]\#[s; 521] & - 16[s; 21]\#[s; 52] & - 13[s; 21]\#[s; 51^2] \\
& - 22[s; 21]\#[s; 51] & - 16[s; 21]\#[s; 5] & - [s; 21]\#[s; 4^2 1] & - 3[s; 21]\#[s; 4^2] \\
& - 4[s; 21]\#[s; 432] & - 18[s; 21]\#[s; 431] & - 29[s; 21]\#[s; 43] & - 16[s; 21]\#[s; 42^2] \\
& + 3[s; 21]\#[s; 421]\# & - 72[s; 21]\#[s; 421] & - 87[s; 21]\#[s; 42] & + 3[s; 21]\#[s; 41^2]\# \\
& - 82[s; 21]\#[s; 41^2] & - 130[s; 21]\#[s; 41] & - 74[s; 21]\#[s; 4] & - 2[s; 21]\#[s; 3^3] \\
& - 19[s; 21]\#[s; 3^2 2] & + 4[s; 21]\#[s; 3^2 1]\# & - 64[s; 21]\#[s; 3^2 1] & - 69[s; 21]\#[s; 3^2] \\
& + 7[s; 21]\#[s; 32^2]\# & - 72[s; 21]\#[s; 32^2] & + 21[s; 21]\#[s; 321]\# & - 223[s; 21]\#[s; 321] \\
& + 3[s; 21]\#[s; 32]\# & - 250[s; 21]\#[s; 32] & + 32[s; 21]\#[s; 31^2]\# & - 277[s; 21]\#[s; 31^2] \\
& + 3[s; 21]\#[s; 31]\# & - 339[s; 21]\#[s; 31] & - 202[s; 21]\#[s; 3] & + 16[s; 21]\#[s; 2^3]\# \\
& - 93[s; 21]\#[s; 2^3] & + 48[s; 21]\#[s; 2^2 1]\# & - 299[s; 21]\#[s; 2^2 1] & + 8[s; 21]\#[s; 2^2]\# \\
& - 285[s; 21]\#[s; 2^2] & + 60[s; 21]\#[s; 21^2]\# & - 399[s; 21]\#[s; 21^2] & + 13[s; 21]\#[s; 21]\# \\
& - 498[s; 21]\#[s; 21] & + [s; 21]\#[s; 2]\# & - 291[s; 21]\#[s; 2] & + 43[s; 21]\#[s; 1^3]\# \\
& - 252[s; 21]\#[s; 1^3] & + 8[s; 21]\#[s; 1^2]\# & - 311[s; 21]\#[s; 1^2] & + [s; 21]\#[s; 1]\# \\
& - 238[s; 21]\#[s; 1] & - 84[s; 21]\#[s; 0] & + [s; 21][s; 62^2] & + 4[s; 21][s; 621] \\
& + 5[s; 21][s; 62] & + 5[s; 21][s; 61^2] & + 10[s; 21][s; 61] & + 5[s; 21][s; 6] \\
& + 3[s; 21][s; 532] & + 12[s; 21][s; 531] & + 15[s; 21][s; 53] & + 19[s; 21][s; 52^2] \\
& + 57[s; 21][s; 521] & + 71[s; 21][s; 52] & + 76[s; 21][s; 51^2] & + 100[s; 21][s; 51] \\
& + 61[s; 21][s; 5] & + 2[s; 21][s; 4^2 2] & + 8[s; 21][s; 4^2 1] & + 10[s; 21][s; 4^2] \\
& + 3[s; 21][s; 43^2] & + 38[s; 21][s; 432] & + 99[s; 21][s; 431] & + 111[s; 21][s; 43] \\
& - 6[s; 21][s; 42^2]\# & + 120[s; 21][s; 42^2] & - 24[s; 21][s; 421]\# & + 365[s; 21][s; 421] \\
& + 356[s; 21][s; 42] & - 30[s; 21][s; 41^2]\# & + 399[s; 21][s; 41^2] & + 498[s; 21][s; 41] \\
& + 269[s; 21][s; 4] & + 15[s; 21][s; 3^3] & - 6[s; 21][s; 3^2 2]\# & + 115[s; 21][s; 3^2 2] \\
& - 24[s; 21][s; 3^2 1]\# & + 289[s; 21][s; 3^2 1] & + 261[s; 21][s; 3^2] & - 57[s; 21][s; 32^2]\# \\
& + 381[s; 21][s; 32^2] & - 131[s; 21][s; 321]\# & + 1012[s; 21][s; 321] & - 16[s; 21][s; 32]\# \\
& + 942[s; 21][s; 32] & - 158[s; 21][s; 31^2]\# & + 1138[s; 21][s; 31^2] & - 20[s; 21][s; 31]\# \\
& + 1264[s; 21][s; 31] & + 691[s; 21][s; 3] & - 102[s; 21][s; 2^3]\# & + 453[s; 21][s; 2^3] \\
& - 235[s; 21][s; 2^2 1]\# & + 1242[s; 21][s; 2^2 1] & - 41[s; 21][s; 2^2]\# & + 1074[s; 21][s; 2^2] \\
& - 294[s; 21][s; 21^2]\# & + 1610[s; 21][s; 21^2] & - 57[s; 21][s; 21]\# & + 1784[s; 21][s; 21] \\
& - 5[s; 21][s; 2]\# & + 999[s; 21][s; 2] & - 191[s; 21][s; 1^3]\# & + 968[s; 21][s; 1^3] \\
& - 40[s; 21][s; 1^2]\# & + 1115[s; 21][s; 1^2] & - 4[s; 21][s; 1]\# & + 800[s; 21][s; 1] \\
& + 278[s; 21][s; 0] & - [s; 2]\#[s; 53] & - [s; 2]\#[s; 521] & - 2[s; 2]\#[s; 52] \\
& - [s; 2]\#[s; 51^2] & - 3[s; 2]\#[s; 51] & - 2[s; 2]\#[s; 5] & - [s; 2]\#[s; 4^2] \\
& - 4[s; 2]\#[s; 431] & - 6[s; 2]\#[s; 43] & - 3[s; 2]\#[s; 42^2] & - 11[s; 2]\#[s; 421]
\end{aligned}$$

$$\begin{aligned}
& - 18[s; 2] \# [s; 42] & + [s; 2] \# [s; 41^2] \# & - 14[s; 2] \# [s; 41^2] & - 21[s; 2] \# [s; 41] \\
& - 13[s; 2] \# [s; 4] & - 4[s; 2] \# [s; 3^2 2] & - 12[s; 2] \# [s; 3^2 1] & - 17[s; 2] \# [s; 3^2] \\
& - 11[s; 2] \# [s; 32^2] & + 5[s; 2] \# [s; 321] \# & - 47[s; 2] \# [s; 321] & - 49[s; 2] \# [s; 32] \\
& + 5[s; 2] \# [s; 31^2] \# & - 49[s; 2] \# [s; 31^2] & + [s; 2] \# [s; 31] \# & - 67[s; 2] \# [s; 31] \\
& - 36[s; 2] \# [s; 3] & + 3[s; 2] \# [s; 2^3] \# & - 19[s; 2] \# [s; 2^3] & + 8[s; 2] \# [s; 2^2 1] \# \\
& - 57[s; 2] \# [s; 2^2 1] & + 2[s; 2] \# [s; 2^2] \# & - 61[s; 2] \# [s; 2^2] & + 14[s; 2] \# [s; 21^2] \# \\
& - 81[s; 2] \# [s; 21^2] & + 2[s; 2] \# [s; 21] \# & - 95[s; 2] \# [s; 21] & - 57[s; 2] \# [s; 2] \\
& + 8[s; 2] \# [s; 1^3] \# & - 48[s; 2] \# [s; 1^3] & + 2[s; 2] \# [s; 1^2] \# & - 62[s; 2] \# [s; 1^2] \\
& - 44[s; 2] \# [s; 1] & - 16[s; 2] \# [s; 0] & + 2[s; 2] [s; 62^2] & + 4[s; 2] [s; 62 1] \\
& + 4[s; 2] [s; 62] & + 5[s; 2] [s; 61^2] & + 5[s; 2] [s; 61] & + 3[s; 2] [s; 6] \\
& + 5[s; 2] [s; 53 2] & + 11[s; 2] [s; 53 1] & + 11[s; 2] [s; 53] & + 20[s; 2] [s; 52^2] \\
& + 53[s; 2] [s; 52 1] & + 47[s; 2] [s; 52] & + 55[s; 2] [s; 51^2] & + 66[s; 2] [s; 51] \\
& + 31[s; 2] [s; 5] & + 3[s; 2] [s; 4^2 2] & + 7[s; 2] [s; 4^2 1] & + 8[s; 2] [s; 4^2] \\
& + 4[s; 2] [s; 43^2] & + 37[s; 2] [s; 43 2] & + 86[s; 2] [s; 43 1] & + 77[s; 2] [s; 43] \\
& - 9[s; 2] [s; 42^2] \# & + 116[s; 2] [s; 42^2] & - 21[s; 2] [s; 42 1] \# & + 282[s; 2] [s; 42 1] \\
& + 253[s; 2] [s; 42] & - 31[s; 2] [s; 41^2] \# & + 297[s; 2] [s; 41^2] & + 311[s; 2] [s; 41] \\
& + 158[s; 2] [s; 4] & + 14[s; 2] [s; 3^3] & - 8[s; 2] [s; 3^2 2] \# & + 104[s; 2] [s; 3^2 2] \\
& - 20[s; 2] [s; 3^2 1] \# & + 223[s; 2] [s; 3^2 1] & + 188[s; 2] [s; 3^2] & - 54[s; 2] [s; 32^2] \# \\
& + 313[s; 2] [s; 32^2] & - 119[s; 2] [s; 321] \# & + 778[s; 2] [s; 321] & - 13[s; 2] [s; 32] \# \\
& + 635[s; 2] [s; 32] & - 126[s; 2] [s; 31^2] \# & + 790[s; 2] [s; 31^2] & - 19[s; 2] [s; 31] \# \\
& + 816[s; 2] [s; 31] & + 399[s; 2] [s; 3] & - 93[s; 2] [s; 2^3] \# & + 365[s; 2] [s; 2^3] \\
& - 191[s; 2] [s; 2^2 1] \# & + 898[s; 2] [s; 2^2 1] & - 36[s; 2] [s; 2^2] \# & + 730[s; 2] [s; 2^2] \\
& - 234[s; 2] [s; 21^2] \# & + 1111[s; 2] [s; 21^2] & - 45[s; 2] [s; 21] \# & + 1115[s; 2] [s; 21] \\
& - 4[s; 2] [s; 2] \# & + 585[s; 2] [s; 2] & - 140[s; 2] [s; 1^3] \# & + 631[s; 2] [s; 1^3] \\
& - 32[s; 2] [s; 1^2] \# & + 681[s; 2] [s; 1^2] & - 3[s; 2] [s; 1] \# & + 447[s; 2] [s; 1] \\
& + 149[s; 2] [s; 0] & - [s; 1^2] \# [s; 62] & - [s; 1^2] \# [s; 61] & - [s; 1^2] \# [s; 53 1] \\
& - 5[s; 1^2] \# [s; 53] & - [s; 1^2] \# [s; 52^2] & - 8[s; 1^2] \# [s; 52 1] & - 11[s; 1^2] \# [s; 52] \\
& - 7[s; 1^2] \# [s; 51^2] & - 14[s; 1^2] \# [s; 51] & - 7[s; 1^2] \# [s; 5] & - [s; 1^2] \# [s; 4^2 1] \\
& - 4[s; 1^2] \# [s; 4^2] & - [s; 1^2] \# [s; 43^2] & - 5[s; 1^2] \# [s; 43 2] & - 22[s; 1^2] \# [s; 43 1] \\
& - 24[s; 1^2] \# [s; 43] & + [s; 1^2] \# [s; 42^2] \# & - 19[s; 1^2] \# [s; 42^2] & + 3[s; 1^2] \# [s; 42 1] \# \\
& - 55[s; 1^2] \# [s; 42 1] & - 67[s; 1^2] \# [s; 42] & + 3[s; 1^2] \# [s; 41^2] \# & - 59[s; 1^2] \# [s; 41^2] \\
& - 74[s; 1^2] \# [s; 41] & - 39[s; 1^2] \# [s; 4] & - 3[s; 1^2] \# [s; 3^3] & + [s; 1^2] \# [s; 3^2 2] \# \\
& - 24[s; 1^2] \# [s; 3^2 2] & + 4[s; 1^2] \# [s; 3^2 1] \# & - 55[s; 1^2] \# [s; 3^2 1] & - 60[s; 1^2] \# [s; 3^2] \\
& + 9[s; 1^2] \# [s; 32^2] \# & - 63[s; 1^2] \# [s; 32^2] & + 24[s; 1^2] \# [s; 32 1] \# & - 183[s; 1^2] \# [s; 32 1] \\
& + 3[s; 1^2] \# [s; 32] \# & - 166[s; 1^2] \# [s; 32] & + 21[s; 1^2] \# [s; 31^2] \# & - 172[s; 1^2] \# [s; 31^2] \\
& + 3[s; 1^2] \# [s; 31] \# & - 206[s; 1^2] \# [s; 31] & - 102[s; 1^2] \# [s; 3] & + 19[s; 1^2] \# [s; 2^3] \# \\
& - 79[s; 1^2] \# [s; 2^3] & + 39[s; 1^2] \# [s; 2^2 1] \# & - 204[s; 1^2] \# [s; 2^2 1] & + 9[s; 1^2] \# [s; 2^2] \# \\
& - 186[s; 1^2] \# [s; 2^2] & + 42[s; 1^2] \# [s; 21^2] \# & - 248[s; 1^2] \# [s; 21^2] & + 8[s; 1^2] \# [s; 21] \# \\
& - 269[s; 1^2] \# [s; 21] & + [s; 1^2] \# [s; 2] \# & - 143[s; 1^2] \# [s; 2] & + 21[s; 1^2] \# [s; 1^3] \# \\
& - 131[s; 1^2] \# [s; 1^3] & + 4[s; 1^2] \# [s; 1^2] \# & - 158[s; 1^2] \# [s; 1^2] & - 103[s; 1^2] \# [s; 1] \\
& - 32[s; 1^2] \# [s; 0] & + [s; 1^2] [s; 62^2] & + 3[s; 1^2] [s; 62 1] & + 4[s; 1^2] [s; 62] \\
& + 4[s; 1^2] [s; 61^2] & + 5[s; 1^2] [s; 61] & + 2[s; 1^2] [s; 6] & + 4[s; 1^2] [s; 53 2] \\
& + 10[s; 1^2] [s; 53 1] & + 15[s; 1^2] [s; 53] & + 17[s; 1^2] [s; 52^2] & + 48[s; 1^2] [s; 52 1] \\
& + 47[s; 1^2] [s; 52] & + 47[s; 1^2] [s; 51^2] & + 61[s; 1^2] [s; 51] & + 29[s; 1^2] [s; 5] \\
& + 3[s; 1^2] [s; 4^2 2] & + 7[s; 1^2] [s; 4^2 1] & + 9[s; 1^2] [s; 4^2] & + 5[s; 1^2] [s; 43^2] \\
& + 37[s; 1^2] [s; 43 2] & + 90[s; 1^2] [s; 43 1] & + 83[s; 1^2] [s; 43] & - 9[s; 1^2] [s; 42^2] \# \\
& + 108[s; 1^2] [s; 42^2] & - 21[s; 1^2] [s; 42 1] \# & + 268[s; 1^2] [s; 42 1] & + 250[s; 1^2] [s; 42] \\
& - 22[s; 1^2] [s; 41^2] \# & + 268[s; 1^2] [s; 41^2] & + 291[s; 1^2] [s; 41] & + 143[s; 1^2] [s; 4] \\
& + 16[s; 1^2] [s; 3^3] & - 10[s; 1^2] [s; 3^2 2] \# & + 112[s; 1^2] [s; 3^2 2] & - 22[s; 1^2] [s; 3^2 1] \# \\
& + 227[s; 1^2] [s; 3^2 1] & + 195[s; 1^2] [s; 3^2] & - 57[s; 1^2] [s; 32^2] \# & + 307[s; 1^2] [s; 32^2]
\end{aligned}$$

$$\begin{aligned}
& - 114[s; 1^2][s; 321]\# & + 746[s; 1^2][s; 321] & - 15[s; 1^2][s; 32]\# & + 614[s; 1^2][s; 32] \\
& - 108[s; 1^2][s; 31^2]\# & + 718[s; 1^2][s; 31^2] & - 15[s; 1^2][s; 31]\# & + 757[s; 1^2][s; 31] \\
& + 364[s; 1^2][s; 3] & - 96[s; 1^2][s; 2^3]\# & + 351[s; 1^2][s; 2^3] & - 181[s; 1^2][s; 2^2 1]\# \\
& + 837[s; 1^2][s; 2^2 1] & - 35[s; 1^2][s; 2^2]\# & + 676[s; 1^2][s; 2^2] & - 196[s; 1^2][s; 21^2]\# \\
& + 991[s; 1^2][s; 21^2] & - 37[s; 1^2][s; 21]\# & + 999[s; 1^2][s; 21] & - 4[s; 1^2][s; 2]\# \\
& + 516[s; 1^2][s; 2] & - 106[s; 1^2][s; 1^3]\# & + 534[s; 1^2][s; 1^3] & - 21[s; 1^2][s; 1^2]\# \\
& + 585[s; 1^2][s; 1^2] & - [s; 1^2][s; 1]\# & + 379[s; 1^2][s; 1] & + 119[s; 1^2][s; 0] \\
& - [s; 1]\#[s; 53] & - [s; 1]\#[s; 521] & - 2[s; 1]\#[s; 52] & - [s; 1]\#[s; 51^2] \\
& - 2[s; 1]\#[s; 51] & - [s; 1]\#[s; 5] & - [s; 1]\#[s; 4^2] & - [s; 1]\#[s; 432] \\
& - 5[s; 1]\#[s; 431] & - 6[s; 1]\#[s; 43] & - 3[s; 1]\#[s; 42^2] & + [s; 1]\#[s; 421]\# \\
& - 12[s; 1]\#[s; 421] & - 15[s; 1]\#[s; 42] & - 11[s; 1]\#[s; 41^2] & - 16[s; 1]\#[s; 41] \\
& - 7[s; 1]\#[s; 4] & - [s; 1]\#[s; 3^3] & - 5[s; 1]\#[s; 3^2 2] & + [s; 1]\#[s; 3^2 1]\# \\
& - 14[s; 1]\#[s; 3^2 1] & - 15[s; 1]\#[s; 3^2] & + 2[s; 1]\#[s; 32^2]\# & - 14[s; 1]\#[s; 32^2] \\
& + 5[s; 1]\#[s; 321]\# & - 41[s; 1]\#[s; 321] & + [s; 1]\#[s; 32]\# & - 41[s; 1]\#[s; 32] \\
& + 5[s; 1]\#[s; 31^2]\# & - 40[s; 1]\#[s; 31^2] & - 45[s; 1]\#[s; 31] & - 22[s; 1]\#[s; 3] \\
& + 4[s; 1]\#[s; 2^3]\# & - 17[s; 1]\#[s; 2^3] & + 10[s; 1]\#[s; 2^2 1]\# & - 48[s; 1]\#[s; 2^2 1] \\
& + 2[s; 1]\#[s; 2^2]\# & - 43[s; 1]\#[s; 2^2] & + 8[s; 1]\#[s; 21^2]\# & - 53[s; 1]\#[s; 21^2] \\
& + 2[s; 1]\#[s; 21]\# & - 61[s; 1]\#[s; 21] & - 29[s; 1]\#[s; 2] & + 4[s; 1]\#[s; 1^3]\# \\
& - 28[s; 1]\#[s; 1^3] & - 31[s; 1]\#[s; 1^2] & - 20[s; 1]\#[s; 1] & - 5[s; 1]\#[s; 0] \\
& + 2[s; 1][s; 62^2] & + 4[s; 1][s; 621] & + 3[s; 1][s; 62] & + 4[s; 1][s; 61^2] \\
& + 4[s; 1][s; 61] & + [s; 1][s; 6] & + 6[s; 1][s; 532] & + 13[s; 1][s; 531] \\
& + 10[s; 1][s; 53] & + 22[s; 1][s; 52^2] & + 48[s; 1][s; 521] & + 42[s; 1][s; 52] \\
& + 46[s; 1][s; 51^2] & + 47[s; 1][s; 51] & + 20[s; 1][s; 5] & + 4[s; 1][s; 4^2 2] \\
& + 8[s; 1][s; 4^2 1] & + 7[s; 1][s; 4^2] & + 6[s; 1][s; 43^2] & + 44[s; 1][s; 432] \\
& + 86[s; 1][s; 431] & + 73[s; 1][s; 43] & - 12[s; 1][s; 42^2]\# & + 116[s; 1][s; 42^2] \\
& - 26[s; 1][s; 421]\# & + 265[s; 1][s; 421] & + 210[s; 1][s; 42] & - 21[s; 1][s; 41^2]\# \\
& + 236[s; 1][s; 41^2] & + 238[s; 1][s; 41] & + 103[s; 1][s; 4] & + 18[s; 1][s; 3^3] \\
& - 12[s; 1][s; 3^2 2]\# & + 113[s; 1][s; 3^2 2] & - 25[s; 1][s; 3^2 1]\# & + 220[s; 1][s; 3^2 1] \\
& + 165[s; 1][s; 3^2] & - 66[s; 1][s; 32^2]\# & + 312[s; 1][s; 32^2] & - 116[s; 1][s; 321]\# \\
& + 682[s; 1][s; 321] & - 17[s; 1][s; 32]\# & + 528[s; 1][s; 32] & - 107[s; 1][s; 31^2]\# \\
& + 636[s; 1][s; 31^2] & - 13[s; 1][s; 31]\# & + 603[s; 1][s; 31] & + 272[s; 1][s; 3] \\
& - 100[s; 1][s; 2^3]\# & + 336[s; 1][s; 2^3] & - 183[s; 1][s; 2^2 1]\# & + 761[s; 1][s; 2^2 1] \\
& - 35[s; 1][s; 2^2]\# & + 567[s; 1][s; 2^2] & - 182[s; 1][s; 21^2]\# & + 840[s; 1][s; 21^2] \\
& - 36[s; 1][s; 21]\# & + 800[s; 1][s; 21] & - 3[s; 1][s; 2]\# & + 379[s; 1][s; 2] \\
& - 97[s; 1][s; 1^3]\# & + 443[s; 1][s; 1^3] & - 19[s; 1][s; 1^2]\# & + 447[s; 1][s; 1^2] \\
& - [s; 1][s; 1]\# & + 270[s; 1][s; 1] & + 80[s; 1][s; 0] & - [s; 0]\#[s; 431] \\
& - [s; 0]\#[s; 43] & - [s; 0]\#[s; 421] & - 2[s; 0]\#[s; 42] & - [s; 0]\#[s; 41^2] \\
& - [s; 0]\#[s; 41] & - [s; 0]\#[s; 3^2 2] & - 2[s; 0]\#[s; 3^2 1] & - 3[s; 0]\#[s; 3^2] \\
& - [s; 0]\#[s; 32^2] & + [s; 0]\#[s; 321]\# & - 6[s; 0]\#[s; 321] & - 5[s; 0]\#[s; 32] \\
& - 3[s; 0]\#[s; 31^2] & - 5[s; 0]\#[s; 31] & - [s; 0]\#[s; 3] & + [s; 0]\#[s; 2^3]\# \\
& - 2[s; 0]\#[s; 2^3] & + [s; 0]\#[s; 2^2 1]\# & - 5[s; 0]\#[s; 2^2 1] & - 5[s; 0]\#[s; 2^2] \\
& + [s; 0]\#[s; 21^2]\# & - 6[s; 0]\#[s; 21^2] & - 5[s; 0]\#[s; 21] & - 2[s; 0]\#[s; 2] \\
& - 2[s; 0]\#[s; 1^3] & - 3[s; 0]\#[s; 1^2] & - [s; 0]\#[s; 1] & + [s; 0][s; 62^2] \\
& + 2[s; 0][s; 621] & + [s; 0][s; 62] & + 2[s; 0][s; 61^2] & + [s; 0][s; 61] \\
& + 4[s; 0][s; 532] & + 6[s; 0][s; 531] & + 4[s; 0][s; 53] & + 11[s; 0][s; 52^2] \\
& + 22[s; 0][s; 521] & + 16[s; 0][s; 52] & + 18[s; 0][s; 51^2] & + 17[s; 0][s; 51] \\
& + 5[s; 0][s; 5] & + 2[s; 0][s; 4^2 2] & + 4[s; 0][s; 4^2 1] & + 3[s; 0][s; 4^2] \\
& + 4[s; 0][s; 43^2] & + 22[s; 0][s; 432] & + 40[s; 0][s; 431] & + 30[s; 0][s; 43] \\
& - 8[s; 0][s; 42^2]\# & + 56[s; 0][s; 42^2] & - 12[s; 0][s; 421]\# & + 113[s; 0][s; 421]\# \\
& + 82[s; 0][s; 42] & - 9[s; 0][s; 41^2]\# & + 95[s; 0][s; 41^2] & + 84[s; 0][s; 41]
\end{aligned}$$

$$\begin{array}{llll}
+ 32[s; 0][s; 4] & + 9[s; 0][s; 3^3] & - 7[s; 0][s; 3^2 2] \# & + 55[s; 0][s; 3^2 2] \\
- 12[s; 0][s; 3^2 1] \# & + 96[s; 0][s; 3^2 1] & + 69[s; 0][s; 3^2] & - 33[s; 0][s; 32^2] \# \\
+ 140[s; 0][s; 32^2] & - 54[s; 0][s; 321] \# & + 287[s; 0][s; 321] & - 8[s; 0][s; 32] \# \\
+ 204[s; 0][s; 32] & - 44[s; 0][s; 31^2] \# & + 244[s; 0][s; 31^2] & - 5[s; 0][s; 31] \# \\
+ 217[s; 0][s; 31] & + 87[s; 0][s; 3] & - 48[s; 0][s; 2^3] \# & + 145[s; 0][s; 2^3] \\
- 80[s; 0][s; 2^2 1] \# & + 306[s; 0][s; 2^2 1] & - 16[s; 0][s; 2^2] \# & + 215[s; 0][s; 2^2] \\
- 72[s; 0][s; 21^2] \# & + 316[s; 0][s; 21^2] & - 14[s; 0][s; 21] \# & + 278[s; 0][s; 21] \\
- [s; 0][s; 2] \# & + 119[s; 0][s; 2] & - 35[s; 0][s; 1^3] \# & + 155[s; 0][s; 1^3] \\
- 6[s; 0][s; 1^2] \# & + 149[s; 0][s; 1^2] & + 80[s; 0][s; 1] & + 21[s; 0][s; 0]
\end{array}$$

Dimension s;31 = 23,084,400,640

TermSum = 1836

CoeffSum = 108621